

**LANGUAGE EVOLUTION AND  
POPULATION DYNAMICS IN A SYSTEM  
OF TWO INTERACTING SPECIES  
(competition of 2 languages)**

# The Problem

We study the evolution of words and the population dynamics of a system comprising two interacting species which initially speak two different languages using Monte Carlo simulations and assumptions from evolutionary game theory.

# Description of the system

- $A$  and  $B$ , are randomly distributed on a 2D lattice.
- Initially speak **two different languages**.
- $A$  has a common vocabulary of 10 words.
- $B$ , initially a common vocabulary of 10 words, but these words are **different** from the words of  $A$ .
- The species move on the lattice performing random walks.

- Learn words that are unknown to them or forget words that are in their vocabulary.
- Individuals have **fitness**=> measure of their genetic activity.
- Children have an identity and vocabulary identical to their parent.
- Correct communication between individuals increases their fitness.
- Individuals die at a constant rate.

# Some of the Questions we want to answer

- Will a difference in the initial fitness lead to a permanent advantage?
- Will this advantage affect the vocabulary of the species or the population dynamics?
- How will the spatial distributions of the species be affected?
- Does the system exhibit pattern formation or segregation?

# Monte Carlo Method

- Individuals have an Identity (A or B species) and a vocabulary of 10 words. Activities allowed: Movement, communication, reproduction and mortality.
- We draw Random Numbers in order to decide about:
- **Movement**: Random motion ( Diffusion) on a rectangular lattice.
- **Communication**: Individuals meet and may learn words known to their neighbor or forget words unknown to their neighbor. Correct communication conveys a payoff which increases the fitness of the individual.

- **Reproduction:** The probability of reproduction for an individual is proportional to the individual fitness. Normalization of the probability is either local (in the 8 closest neighbors of the individual) or global (over the complete lattice). Offspring inherit the parental identity and vocabulary.
- Results presented below follow the local normalization choice.
- **Mortality:** Individuals die at a constant rate. For our present results the average lifetime of an individual is 19 Monte Carlo Steps (MCS)

# Initial Vocabulary

1	1	1	1	1	1	1	1	1	1	0	0	0	0	0	0	0	0	0	0
---	---	---	---	---	---	---	---	---	---	---	---	---	---	---	---	---	---	---	---

Species A at time  $t=0$

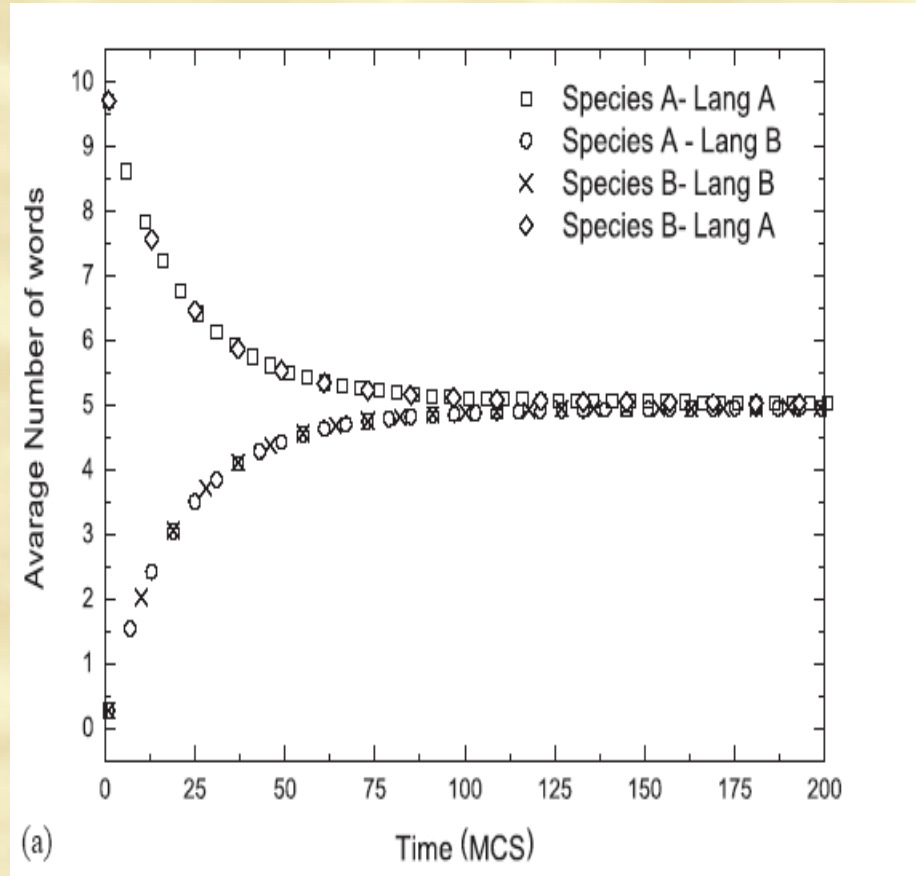
0	0	0	0	0	0	0	0	0	0	1	1	1	1	1	1	1	1	1	1
---	---	---	---	---	---	---	---	---	---	---	---	---	---	---	---	---	---	---	---

Species B at time  $t=0$



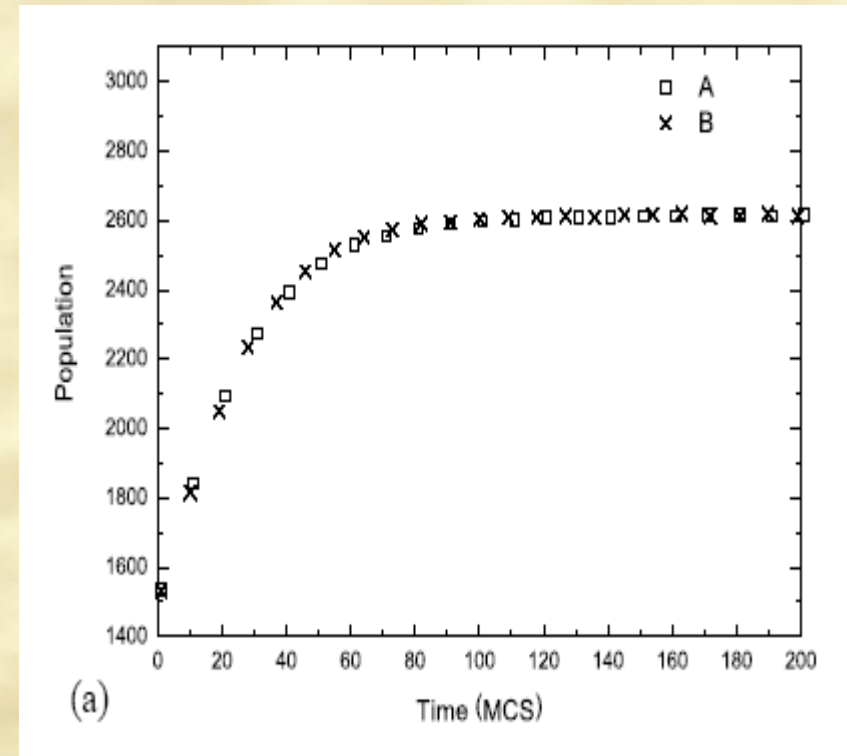
# Homogeneous system with constant number of individuals

- Number A = Number B
- Fitness A = Fitness B
- No Reproduction or Death



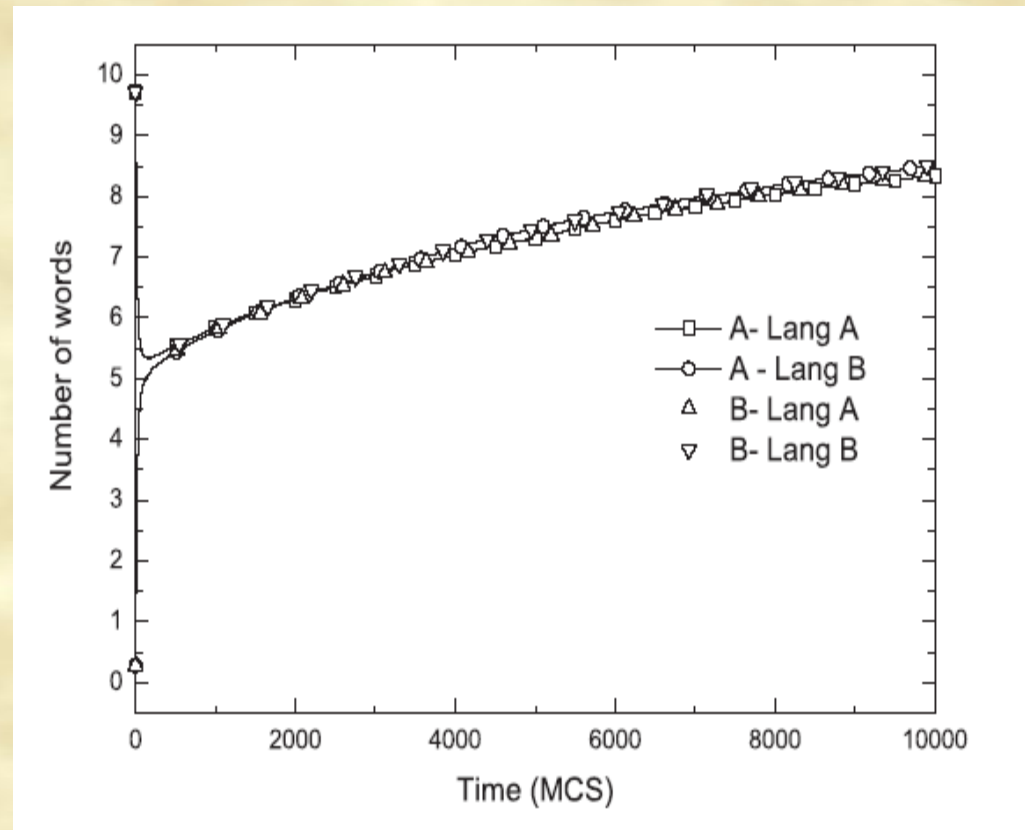
# Homogenous System with variable number of individuals

- A system where the number of A's is the same as the initial number of B's and reproduction and mortality is allowed. Then:
- The average population of the A species equals that of B, and is determined by the size of the system.



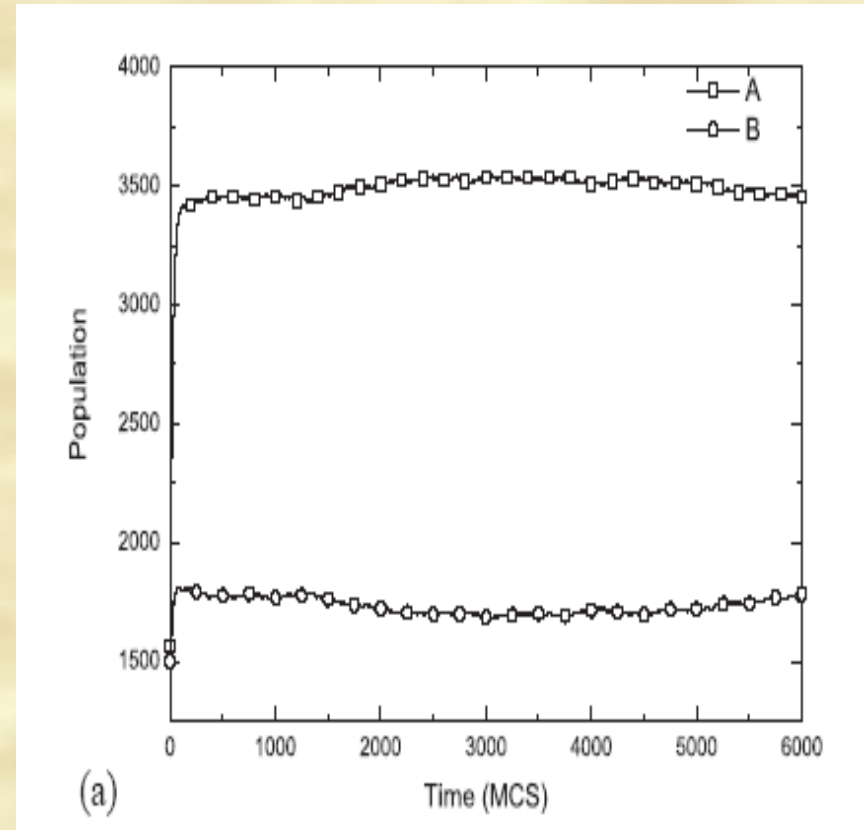
# Homogenous System with variable number of individuals

The species start with a vocabulary of 10 words and end up with a vocabulary of (on average) 19.7 words, i.e. the system becomes bilingual.



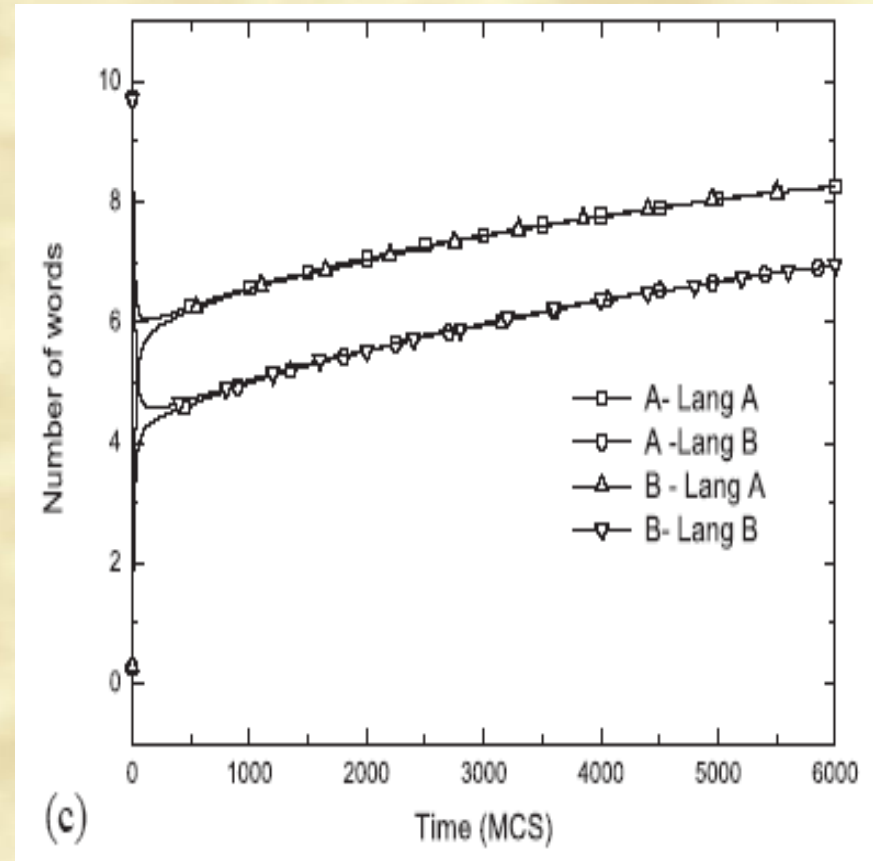
# Inhomogeneous System (Different initial Fitness)

- A system where initially the A's and the B's are equal in number but the A's have higher initial fitness.
- The initial fitness advantage leads to numerical superiority for the A's.



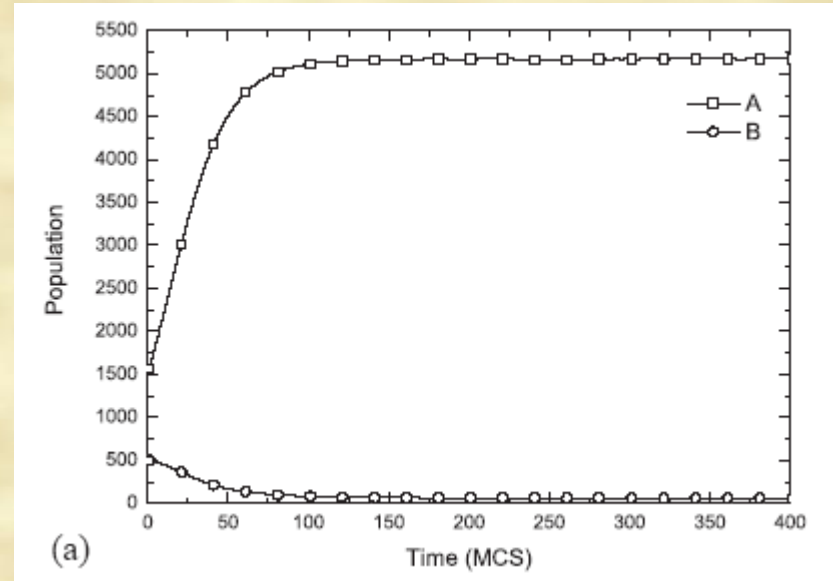
# Inhomogeneous System (Different initial Fitness)

- For a long time interval, an average individual knows slightly more words of the A Language than of the B Language.
- The B language survives and finally the system is bilingual.



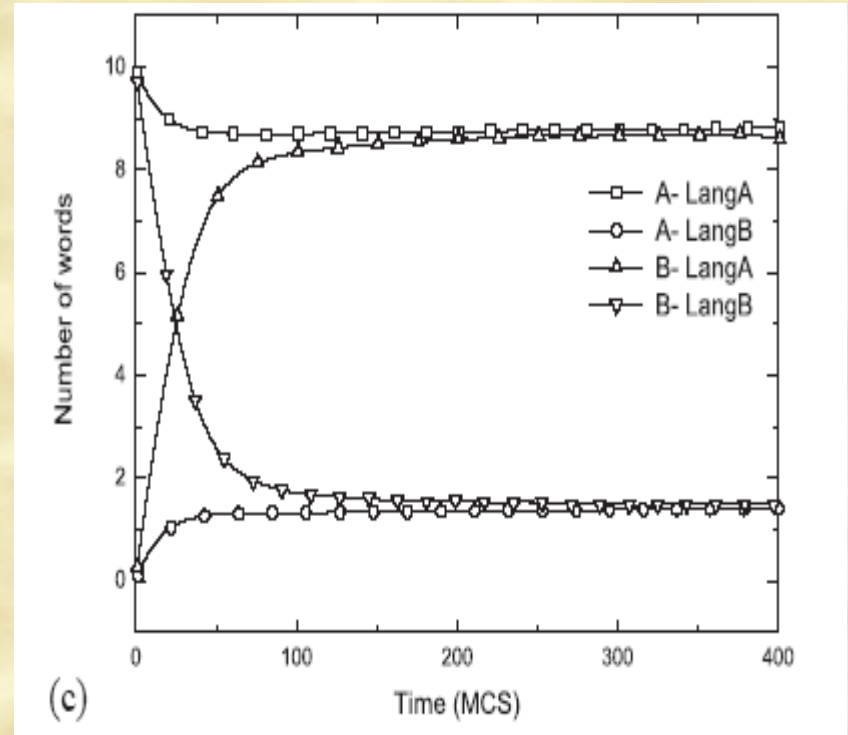
# Highly Inhomogeneous System

- For a system where initially the A's greatly outnumber the B's in *number and fitness*
- The population of the B's rapidly vanishes.



# Highly Inhomogeneous System

- Some words of Language B survive in the vocabulary of species A
- A richer language containing synonyms is created.



# SEGREGATION

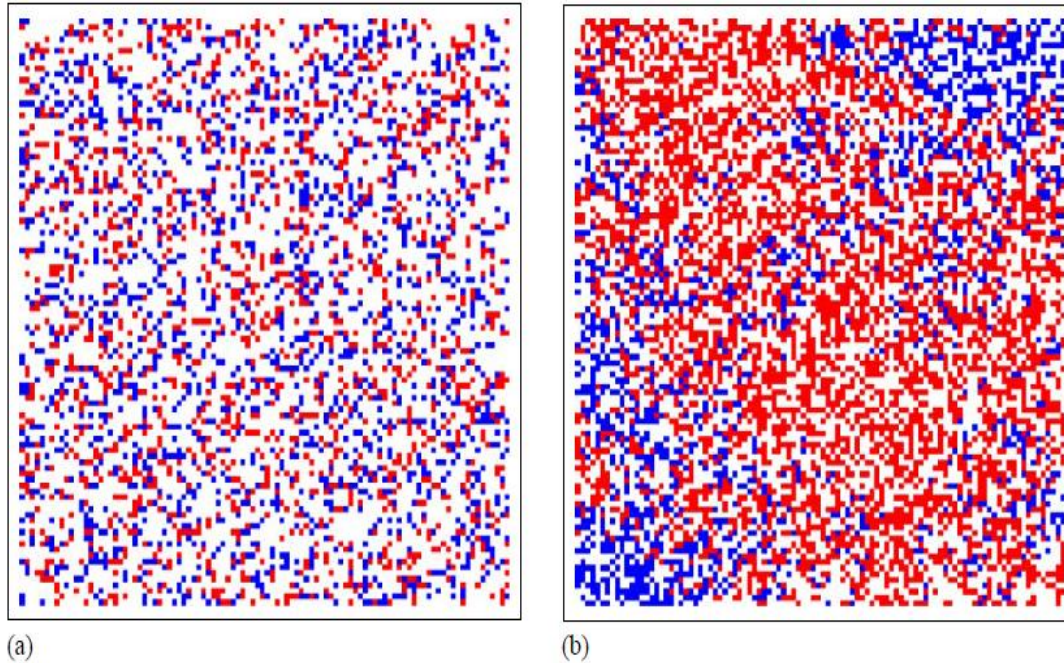


Fig. 7. A snapshot of the system at time  $t = 1$  MCS (a) and at time  $t = 10000$  MCS (b). Red sites are occupied by  $A$  individuals while blue sites by  $B$  individuals. The initial concentration of the species is  $c_A = 0.15$  and  $c_B = 0.15$ . The initial fitness of the  $A$  species is  $f_A = 30$  units and the initial fitness of the  $B$  species  $f_B = 30$  units (particle size not to scale)



# CONCLUSIONS

- When none of the species has no initial genetic advantage (or a small genetic advantage) both species end bilingual.
- Total number of words is the maximum possible.
- When one of the species comprises from rather few individuals with small initial fitness then it is quickly lead to extinction. A part of their vocabulary however survives and the final state of the system practically consists that of one species speaking a “richer” language containing *synonyms*.

# Vocabulary on a scale –free network

- Why Scale-free ?
- Traditionally a 2D lattice is adequate.
- Modern technologies facilitate long range interactions: An acquaintance in China may be equally important to a next door neighbor.

# SCALE FREE NETWORKS

- Individuals are nodes on a graph, linked only if they know each other.
- Several social networks have a degree distribution  $p(k) \sim k^{-\gamma}$
- Scale-free networks,  $\Rightarrow$  existence of nodes with very high degree (“hubs”)

# MONTE CARLO SIMULATIONS

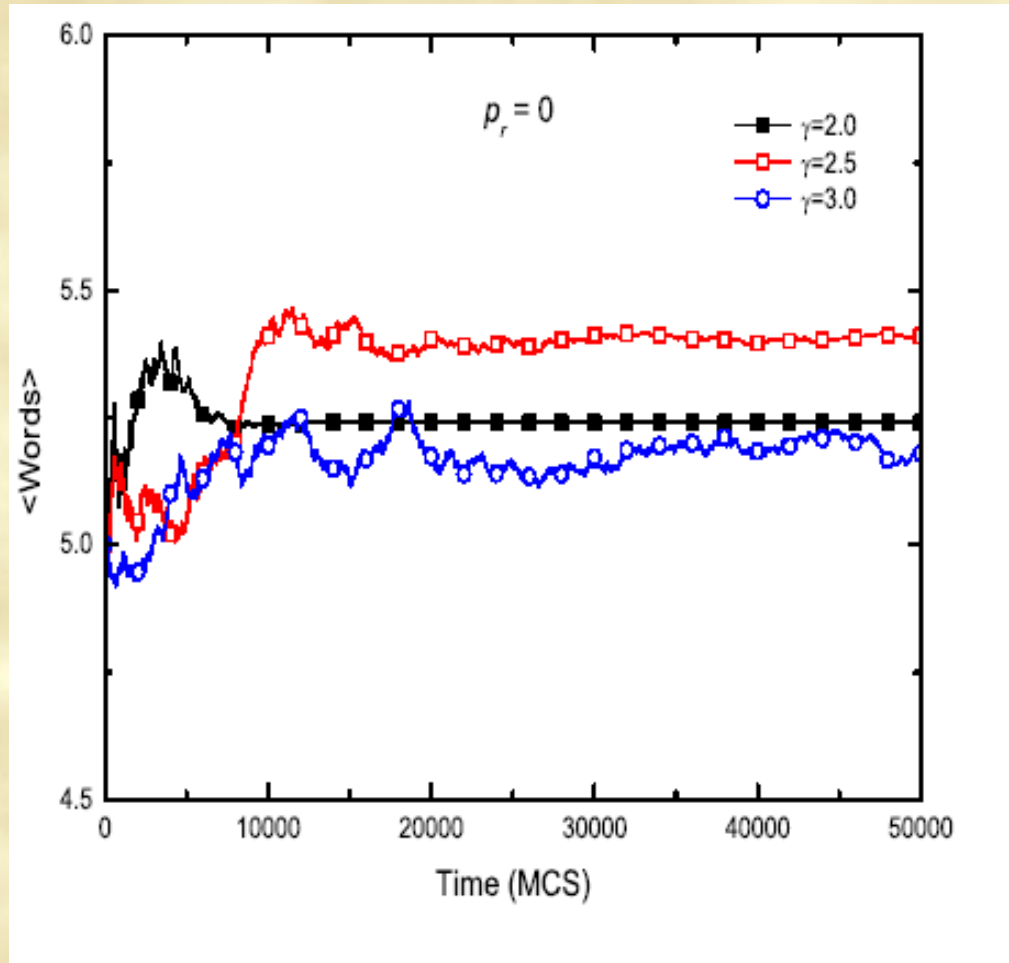
- Individuals are nodes on a scale free network
- Each has a maximum vocabulary of 10 words.
- Initially individuals know on average 5 words, randomly chosen out of the 10 possible.

# MONTE CARLO SIMULATIONS

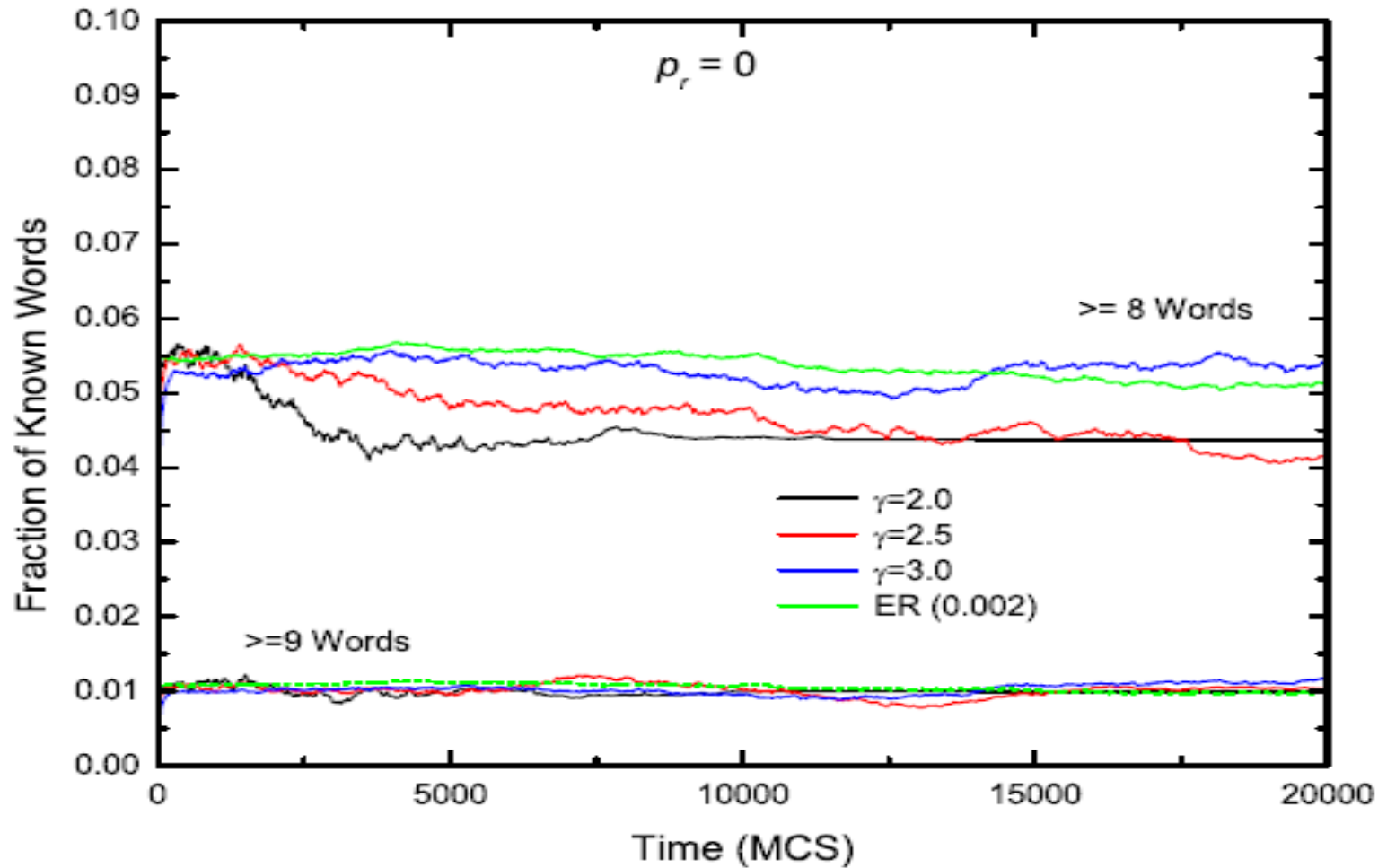
- They communicate with their neighbors, gaining fitness.
- They may learn new words from their neighbors, with probability  $P_L$
- They may forget words not known to their neighbors, with probability  $P_f$ .
- Reproduction probability proportional to fitness.
- Child replaces a randomly selected node.
- Child has the fitness of the parent.

# *No Reproduction*

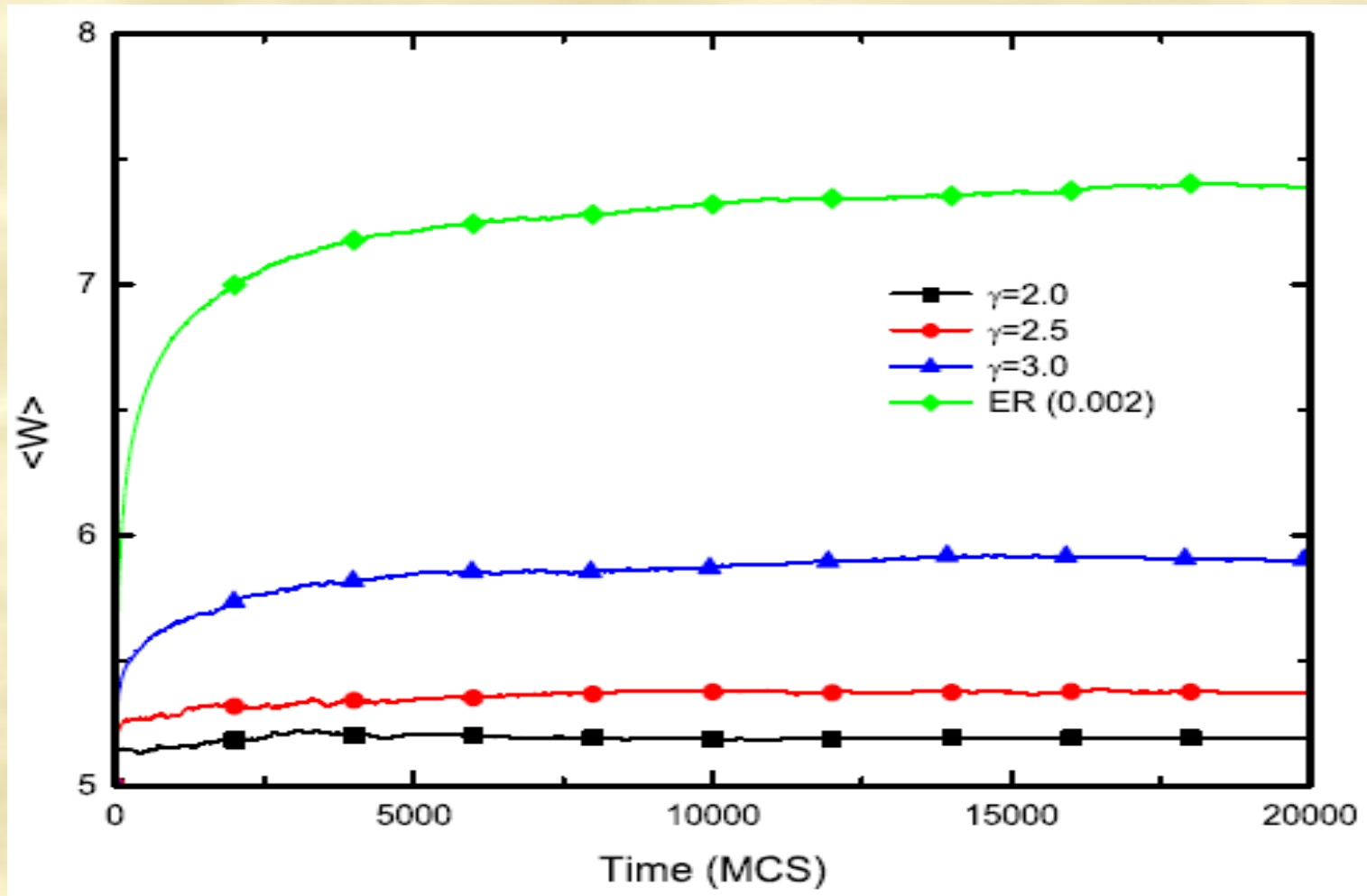
Average number of words = Initial number of words.



# *No Reproduction*



# Reproduction

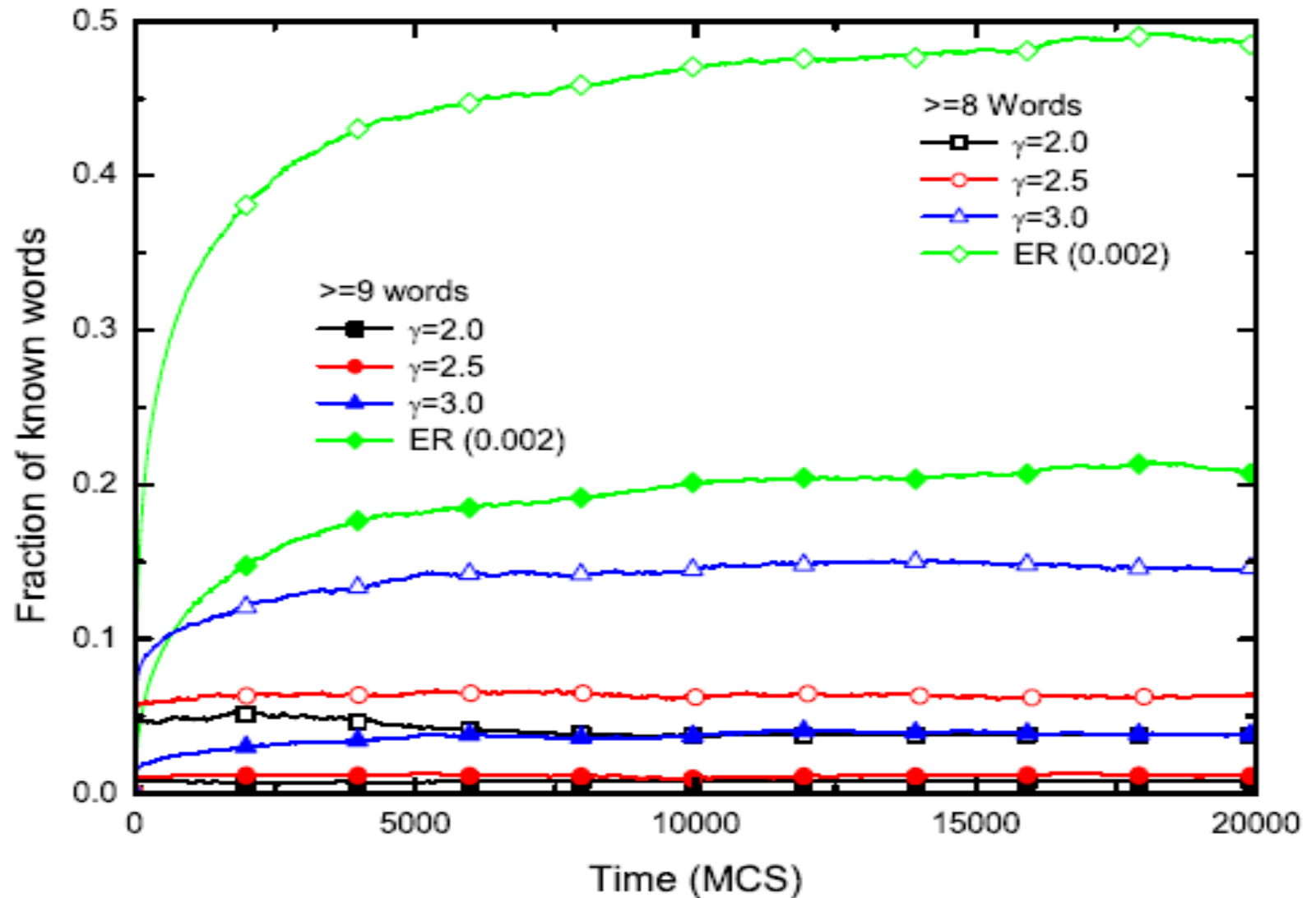




# Reproduction

- Especially for  $\gamma=2.0$ , the number of words is quite below the maximum vocabulary size.
- The reason for this is that in such a network there are several hubs.
- A new fitness generating mechanism=>Knowing the words of hubs.

# Reproduction



# CONCLUSION

- On scale-free networks it is not necessary to know everything.
- Survival chances are increased by using the vocabulary of the “hubs” .
- The existence of the “hubs” in a scale-free network is the source of an additional important fitness generating mechanism.